

Warm Up # 10-1

1. In a class of 40 students, 19 play team sports, 20 run track and 8 do neither. Find the probability that a student randomly chosen from this class

- a) plays team sports
- b) does not run track
- c) does at least one of these
- d) plays team sports, but doesn't run track
- e) does only one of these

HW Questions:

Answers are after the HW slide.

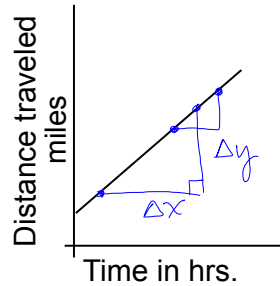
## Review Rates of Change

A comparison between 2 different types of quantities

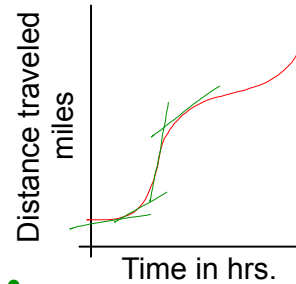
Example: points per game

inches of rain per day

miles per hour



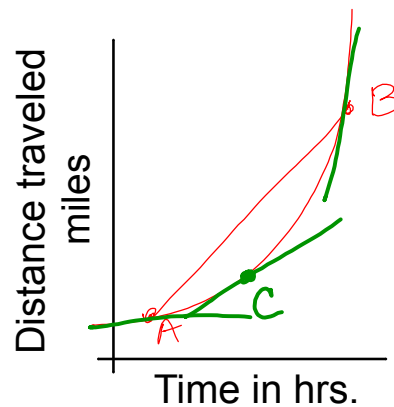
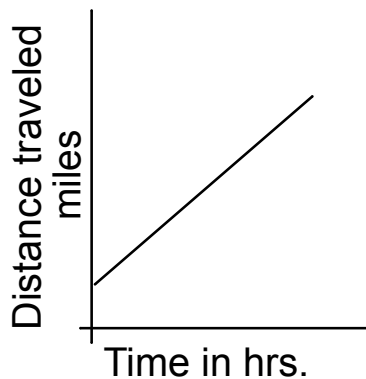
constant rate  
of change



Rate of change is  
changing

$$\text{Average Rate of Change} = \frac{\Delta y}{\Delta x}$$

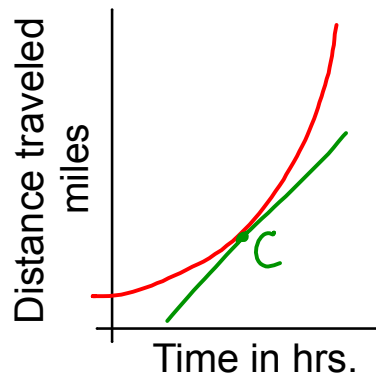
slope between  
2 points



## Instantaneous Rate of Change

The rate of change at a particular point

This rate of change = slope of the tangent line at that point.



## Introduction to Differential Calculus

### Vocabulary:

Gradient  $\rightarrow$  Slope  $\rightarrow \frac{\Delta y}{\Delta x}$

Derivative  $\rightarrow$  Rate of change anywhere on the curve, which = slope of the tangent line at any point on the curve.

### Differentiation

The process of finding the derivative.

## Differentiation

$$y = ax^n$$

Derivative:  $y' = a \cdot n x^{n-1}$

Slope of  
tangent

$$y = 2x^1$$

$$y' = 2(1)x^{1-1}$$

Example:  $y = 2x$

$$y' = 2x^0$$

$$y' = 2$$

$$y = 2x + 5$$

$$y' = 2$$

$y = x^2$

$$y' = (1)(2)x^{2-1}$$

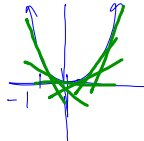
$$y' = 2x \quad @ x = -1 \quad \text{slope} = -2$$

$$@ x = 0$$

$$\text{slope} = 2(0) = 0$$

$$@ x = 2$$

$$\text{slope} = 2(2) = 4$$



For tonight's homework:

### Formal Laws of Probability

Addition Law  $\rightarrow P(A) + P(B) - P(A \cap B) = P(A \cup B)$

intersection  
Both A and B

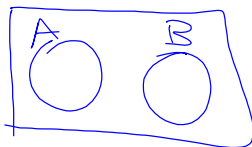
Union

Mutually Exclusive = Disjoint

A & B have no elements  
in common

Either A or B  
or both

$$P(A \cap B) = 0$$



$$P(A) + P(B) = P(A \cup B)$$

# HW: 9I p. 290, # 1 - 5

## HW Quiz tomorrow:

9F p. 279

9F p. 280

9G.2 & 9G.3, p. 284-285

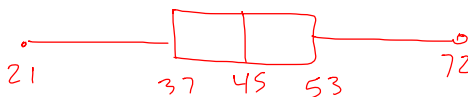
Rev. Set 9B p. 296

### Answers to IB Test Practice (2008 paper 1)

2. a) 45

b) 16

c) box plot

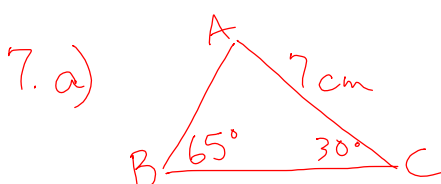


1. a) 29.7675

b)  $\approx 30$

c)  $\approx 0.781\%$

d)  $7.81 \times 10^{-1}$



7b)  $AB \approx 3.86 \text{ cm}$

c)  $\text{Area} \approx 13.5 \text{ cm}^2$

5a) variables are independent... (detail complete sentence)

$$b) df = (3-1)(3-1) \\ = 4$$

$$c) \chi^2 \approx 51.6$$

$$d) p \approx 1.71 \times 10^{-10}$$

Since  $p < 0.05$   
we reject  $H_0$

$$9b) 3800 \leq w < 4000$$

$$c) \frac{3}{35} \approx 0.0857$$

9a) Histogram  
bars are  
connected.